

MATH 116 — PRACTICE FOR EXAM 1

Generated February 15, 2021

NAME: _____

INSTRUCTOR: _____ SECTION NUMBER: _____

1. This exam has 4 questions. Note that the problems are not of equal difficulty, so you may want to skip over and return to a problem on which you are stuck.
2. Do not separate the pages of the exam. If any pages do become separated, write your name on them and point them out to your instructor when you hand in the exam.
3. Please read the instructions for each individual exercise carefully. One of the skills being tested on this exam is your ability to interpret questions, so instructors will not answer questions about exam problems during the exam.
4. Show an appropriate amount of work (including appropriate explanation) for each exercise so that the graders can see not only the answer but also how you obtained it. Include units in your answers where appropriate.
5. You may use any calculator except a TI-92 (or other calculator with a full alphanumeric keypad). However, you must show work for any calculation which we have learned how to do in this course. You are also allowed two sides of a $3'' \times 5''$ note card.
6. If you use graphs or tables to obtain an answer, be certain to include an explanation and sketch of the graph, and to write out the entries of the table that you use.
7. You must use the methods learned in this course to solve all problems.

Semester	Exam	Problem	Name	Points	Score
Winter 2016	1	7	jewelry	10	
Winter 2017	1	6	Rodin Coil	10	
Winter 2010	3	4		8	
Winter 2013	1	7		8	
Total				36	

Recommended time (based on points): 35 minutes

7. [10 points] Maize and Blue Jewelry Company is trying to decide on a design for their signature aMaize-ing bracelet. There are two possible designs: type W and type J . The company has done research and the two bracelet designs are equally pleasing to customers. The design for both rings starts with the function $C(x) = \cos\left(\frac{\pi}{2}x\right)$ where all units are in millimeters. Let R be the region enclosed by the graph of $C(x)$ and the graph of $-C(x)$ for $-1 \leq x \leq 1$.
- a. [5 points] The type W bracelet is in the shape of the solid formed by rotating R around the line $x = 50$. Write an integral that gives the volume of the type W bracelet. Include **units**.
- b. [5 points] The type J bracelet is in the shape of the solid formed by rotating R around the line $y = -50$. Write an integral that gives the volume of the type J bracelet. Include **units**.

6. [10 points] The Rodin Coil is a fantastic device that (supposedly) creates unlimited free energy. The rate at which it creates this energy is a function of the volume of the coil.

a. [5 points] Suppose a prototype of the Rodin Coil is the solid whose base is the circle $x^2 + y^2 = 2$ (where x and y are measured in meters), and whose cross sections perpendicular to the x -axis are squares. Write, but do **not** compute, an expression involving one or more integrals which gives the volume, in cubic meters, of this prototype.

b. [5 points] One of Rodin's students was able to come up with an even more efficient free energy machine. Suppose the student's prototype was made by taking the same circle $x^2 + y^2 = 2$ and rotating it around the vertical line $x = 3$. Write, but do **not** compute, an expression involving one or more integrals which gives the volume, in cubic meters, of this prototype.

4. [8 points] Consider a solid whose base is contained between the curves $y = e^x$, $y = 1$, and $x = 3$. Cross-sectional slices perpendicular to the x-axis are rectangles, having length contained in the base region mentioned above and height determined by $g(x) = x^2$. Determine the exact volume of this solid.

7. [8 points] Let S be the solid whose base is the region bounded by the curves $y = x^2$, $y = 6 - x$ and $x = 0$ and whose cross sections **parallel** to the x -axis are squares. Find a formula involving definite integrals that computes the volume of S .

